

Good Fair Poor

## Searching

| Algorithm  | Data Structure                            | Time Complexity           |                           | Space Complexity |
|--|---|---------------------------|---------------------------|------------------|
|  |   | Average                   | Worst                     | Worst            |
| <a href="#">Depth First Search (DFS)</a>   | Graph of $ V $ vertices and $ E $ edges   |                           | $O( E  +  V )$            | $O( V )$         |
| <a href="#">Breadth First Search (BFS)</a>   | Graph of $ V $ vertices and $ E $ edges   |                           | $O( E  +  V )$            | $O( V )$         |
| <a href="#">Binary search</a>  | Sorted array of $n$ elements              | $O(\log(n))$              | $O(\log(n))$              | $O(1)$           |
| <a href="#">Linear (Brute Force)</a>   | Array                                     | $O(n)$                    | $O(n)$                    | $O(1)$           |
| <a href="#">Shortest path by Dijkstra, using a Min-heap as priority queue</a>        | Graph with $ V $ vertices and $ E $ edges | $O(( V  +  E ) \log  V )$ | $O(( V  +  E ) \log  V )$ | $O( V )$         |
| <a href="#">Shortest path by Dijkstra, using an unsorted array as priority queue</a> | Graph with $ V $ vertices and $ E $ edges | $O( V ^2)$                | $O( V ^2)$                | $O( V )$         |
| <a href="#">Shortest path by Bellman-Ford</a>  | Graph with $ V $ vertices and $ E $ edges | $O( V  E )$               | $O( V  E )$               | $O( V )$         |

## Sorting

| Algorithm                      | Data Structure | Time Complexity |                |                | Worst Case Auxiliary Space Complexity |
|--------------------------------|----------------|-----------------|----------------|----------------|---------------------------------------|
|                                |                | Best            | Average        | Worst          | Worst                                 |
| <a href="#">Quicksort</a>      | Array          | $O(n \log(n))$  | $O(n \log(n))$ | $O(n^2)$       | $O(n)$                                |
| <a href="#">Mergesort</a>      | Array          | $O(n \log(n))$  | $O(n \log(n))$ | $O(n \log(n))$ | $O(n)$                                |
| <a href="#">Heapsort</a>       | Array          | $O(n \log(n))$  | $O(n \log(n))$ | $O(n \log(n))$ | $O(1)$                                |
| <a href="#">Bubble Sort</a>    | Array          | $O(n)$          | $O(n^2)$       | $O(n^2)$       | $O(1)$                                |
| <a href="#">Insertion Sort</a> | Array          | $O(n)$          | $O(n^2)$       | $O(n^2)$       | $O(1)$                                |
| <a href="#">Select Sort</a>    | Array          | $O(n^2)$        | $O(n^2)$       | $O(n^2)$       | $O(1)$                                |
| <a href="#">Bucket Sort</a>    | Array          | $O(n+k)$        | $O(n+k)$       | $O(n^2)$       | $O(nk)$                               |
| <a href="#">Radix Sort</a>     | Array          | $O(nk)$         | $O(nk)$        | $O(nk)$        | $O(n+k)$                              |

## Data Structures

| Data Structure                     | Time Complexity |              |              |              |              |              |              |              | Space Complexity Worst |
|------------------------------------|-----------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|------------------------|
|                                    | Average         |              |              |              | Worst        |              |              |              |                        |
|                                    | Indexing        | Search       | Insertion    | Deletion     | Indexing     | Search       | Insertion    | Deletion     |                        |
| <a href="#">Basic Array</a>        | $O(1)$          | $O(n)$       | -            | -            | $O(1)$       | $O(n)$       | -            | -            | $O(n)$                 |
| <a href="#">Dynamic Array</a>      | $O(1)$          | $O(n)$       | $O(n)$       | $O(n)$       | $O(1)$       | $O(n)$       | $O(n)$       | $O(n)$       | $O(n)$                 |
| <a href="#">Singly-Linked List</a> | $O(n)$          | $O(n)$       | $O(1)$       | $O(1)$       | $O(n)$       | $O(n)$       | $O(1)$       | $O(1)$       | $O(n)$                 |
| <a href="#">Doubly-Linked List</a> | $O(n)$          | $O(n)$       | $O(1)$       | $O(1)$       | $O(n)$       | $O(n)$       | $O(1)$       | $O(1)$       | $O(n)$                 |
| <a href="#">Skip List</a>          | $O(\log(n))$    | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$       | $O(n)$       | $O(n)$       | $O(n)$       | $\frac{O(n)}{\log(n)}$ |
| <a href="#">Hash Table</a>         | -               | $O(1)$       | $O(1)$       | $O(1)$       | -            | $O(n)$       | $O(n)$       | $O(n)$       | $O(n)$                 |
| <a href="#">Binary Search Tree</a> | $O(\log(n))$    | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$       | $O(n)$       | $O(n)$       | $O(n)$       | $O(n)$                 |
| <a href="#">Cartesian Tree</a>     | -               | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | -            | $O(n)$       | $O(n)$       | $O(n)$       | $O(n)$                 |
| <a href="#">B-Tree</a>             | $O(\log(n))$    | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$                 |
| <a href="#">Red-Black Tree</a>     | $O(\log(n))$    | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$                 |
| <a href="#">Splay Tree</a>         | -               | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | -            | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$                 |
| <a href="#">AVL Tree</a>           | $O(\log(n))$    | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$                 |

## Heaps

| Heaps                                  | Time Complexity |              |                |              |              |                |              |
|--|-----------------|--------------|----------------|--------------|--------------|----------------|--------------|
|  | Heapify         | Find Max     | Extract Max    | Increase Key | Insert       | Delete         | Merge        |
| <a href="#">Linked List (sorted)</a>   | -               | $O(1)$       | $O(1)$         | $O(n)$       | $O(n)$       | $O(1)$         | $O(m+n)$     |
| <a href="#">Linked List (unsorted)</a> | -               | $O(n)$       | $O(n)$         | $O(1)$       | $O(1)$       | $O(1)$         | $O(1)$       |
| <a href="#">Binary Heap</a>            | $O(n)$          | $O(1)$       | $O(\log(n))$   | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$   | $O(m+n)$     |
| <a href="#">Binomial Heap</a>          | -               | $O(\log(n))$ | $O(\log(n))$   | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$   | $O(\log(n))$ |
| <a href="#">Fibonacci Heap</a>         | -               | $O(1)$       | $O(\log(n))^*$ | $O(1)^*$     | $O(1)$       | $O(\log(n))^*$ | $O(1)$       |

# Graphs

| Node / Edge Management           | Storage            | Add Vertex         | Add Edge           | Remove Vertex      | Remove Edge        | Query    |
|----------------------------------|--------------------|--------------------|--------------------|--------------------|--------------------|----------|
| <a href="#">Adjacency list</a>   | $O( V  +  E )$     | $O(1)$             | $O(1)$             | $O( V  +  E )$     | $O( E )$           | $O( V )$ |
| <a href="#">Incidence list</a>   | $O( V  +  E )$     | $O(1)$             | $O(1)$             | $O( E )$           | $O( E )$           | $O( E )$ |
| <a href="#">Adjacency matrix</a> | $O( V ^2)$         | $O( V ^2)$         | $O(1)$             | $O( V ^2)$         | $O(1)$             | $O(1)$   |
| <a href="#">Incidence matrix</a> | $O( V  \cdot  E )$ | $O( V  \cdot  E )$ | $O( V  \cdot  E )$ | $O( V  \cdot  E )$ | $O( V  \cdot  E )$ | $O( E )$ |

## Notation for asymptotic growth

| letter                 | bound                                 | growth                            |
|------------------------|---------------------------------------|-----------------------------------|
| (theta) $\Theta$       | upper and lower, tight <sup>[1]</sup> | equal <sup>[2]</sup>              |
| (big-oh) $O$           | upper, tightness unknown              | less than or equal <sup>[3]</sup> |
| (small-oh) $o$         | upper, not tight                      | less than                         |
| (big omega) $\Omega$   | lower, tightness unknown              | greater than or equal             |
| (small omega) $\omega$ | lower, not tight                      | greater than                      |

[1] Big O is the upper bound, while Omega is the lower bound. Theta requires both Big O and Omega, so that's why it's referred to as a tight bound (it must be both the upper and lower bound). For example, an algorithm taking  $\Omega(n \log n)$  takes at least  $n \log n$  time but has no upper limit. An algorithm taking  $\Theta(n \log n)$  is far preferential since it takes AT LEAST  $n \log n$  ( $\Omega(n \log n)$ ) and NO MORE THAN  $n \log n$  ( $O(n \log n)$ ).<sup>SO</sup>

[2]  $f(x)=\Theta(g(n))$  means  $f$  (the running time of the algorithm) grows exactly like  $g$  when  $n$  (input size) gets larger. In other words, the growth rate of  $f(x)$  is asymptotically proportional to  $g(n)$ .

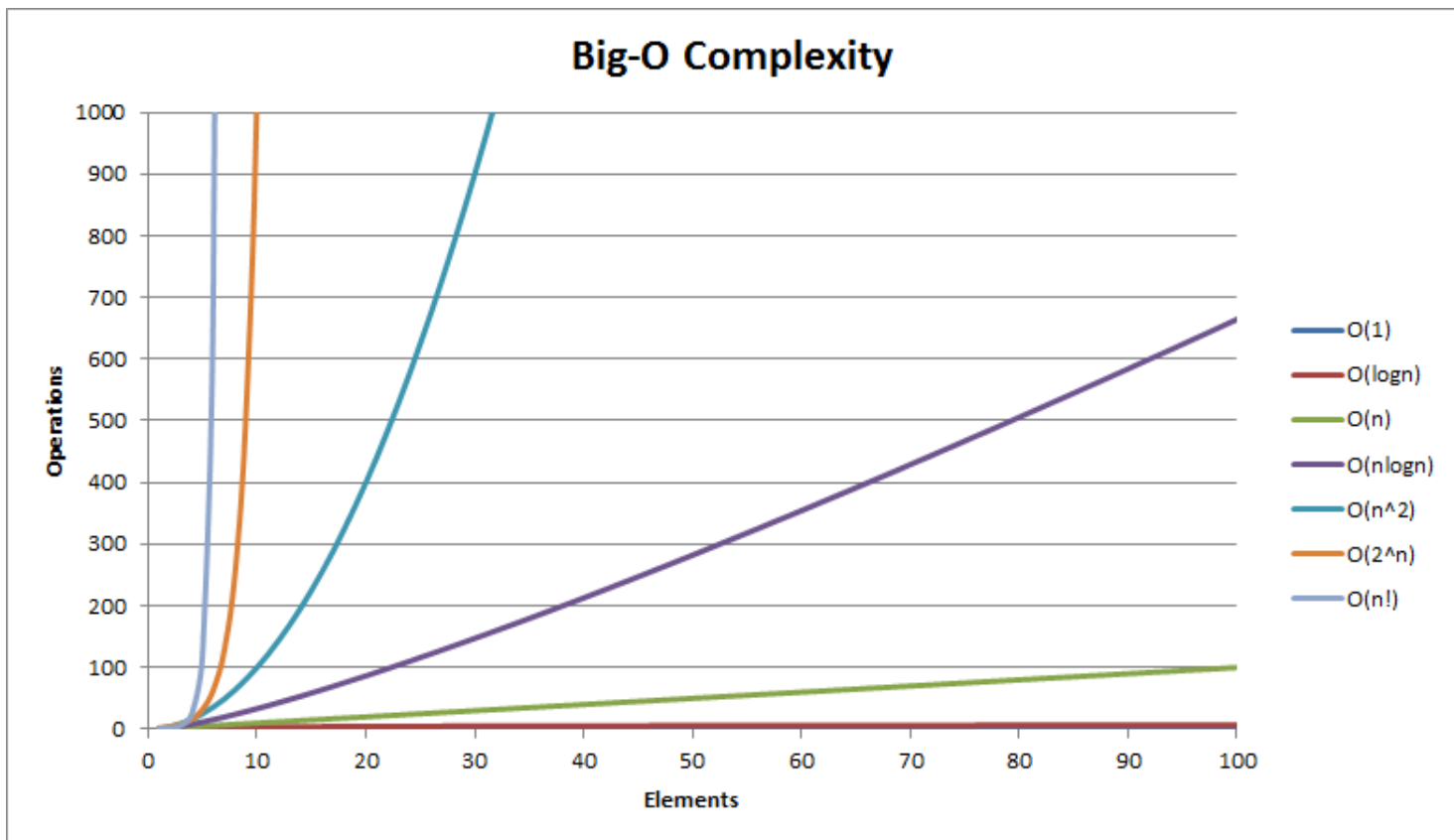
[3] Same thing. Here the growth rate is no faster than  $g(n)$ . big-oh is the most useful because represents the worst-case behavior.

In short, if algorithm is \_\_ then its performance is \_\_

### algorithm performance

|             |          |
|-------------|----------|
| $o(n)$      | $< n$    |
| $O(n)$      | $\leq n$ |
| $\Theta(n)$ | $= n$    |
| $\Omega(n)$ | $\geq n$ |
| $\omega(n)$ | $> n$    |

## Big-O Complexity Chart



## Contribute

[Edit these tables!](#)

Authors:

- [Eric Rowell](#)
- [Quentin Pleple](#)
- [Nick Dizazzo](#)
- [Michael Abed](#)
- [Adam Forsyth](#)
- [Jay Engineer](#)
- [Josh Davis](#)
- [makosblade](#)
- [Alejandro Ramirez](#)
- [Joel Friedly](#)
- [Robert Burke](#)
- [David Dorfman](#)
- [Eric Lefevre-Ardant](#)
- [Thomas Dybdahl Ahle](#)

